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The Effect of Pulse Length and Ejector Radius on Unsteady Ejector Performance

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Abstract

The thrust augmentation of a set of ejectors driven by a shrouded Hartmann-Sprenger tube has been measured at four different frequencies. Each frequency corresponded to a different length to diameter ratio of the pulse of air leaving the driver shroud. Two of the frequencies had length to diameter ratios below the formation number, and two above. The formation number is the value of length to diameter ratio below which the pulse converts to a vortex ring only, and above which the pulse becomes a vortex ring plus a trailing jet.

A three level, three parameter Box-Behnken statistical design of experiment scheme was performed at each frequency, measuring the thrust augmentation generated by the appropriate ejectors from the set. The three parameters were ejector length, radius, and inlet radius.

The results showed that there is an optimum ejector radius and length at each frequency. Using a polynomial fit to the data, the results were interpolated to different ejector radii and pulse length to diameter ratios. This showed that a peak in thrust augmentation occurs when the pulse length to diameter ratio equals the formation number, and that the optimum ejector radius is 0.87 times the sum of the vortex ring radius and the core radius.

Nomenclature

a	radius of vortex ring core
A_{pulse}	exit area of the driving jet
D_{pulse}	$2\sqrt{A_{pulse}/\pi}$ (44 mm)
f	frequency of driving jet
K	circulation in vortex ring
L_{ej}	length of the ejector
L_{pulse}	length of the slug of air in each pulse
\dot{m}_{jet}	mass flow rate of the jet
m_{pulse}	mass of air in each pulse
\dot{m}_{total}	total mass flow rate leaving the ejector
N	formation number
p	fraction of total jet momentum in the vortex ring
R	radius of the vortex ring
R_{ej}	radius of the ejector
R_{exit}	exit radius of the ejector
R_s	inner radius of the shroud (25.4 mm)
r_n	ejector inlet radius
S_t	Strouhal Number (fD_{pulse}/U)
t	time
t	time at which the pulse ratio $L_{pulse}/D_{pulse}=N$
T_{jet}	thrust of jet alone
u(t)	jet velocity as a function of time
U	average velocity of the driving jet = T_{jet}/\dot{m}_{jet}
V_{exit}	average in time and space of ejector exit velocity
α	thrust augmentation coefficient
α_{ss}	thrust augmentation for $L_{pulse}/D_{pulse} = \infty$

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\alpha_{total} weighted sum of \alpha_{ss} and \alpha_{vr} thrust augmentation due to vortex ring only \alpha_{vr}|_{N} \alpha_{vr} for L_{pulse}/D_{pulse} = N
\beta mass entrainment coefficient = (\dot{m}_{total} - \dot{m}_{jet})/\dot{m}_{jet}
\varepsilon a/R
\xi \dot{m}_{jet}/\rho U A_{pulse}
\rho atmospheric air density
\tau period of one pulse = 1/f
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I. Introduction

The current interest in Pulsed Detonation Engines has revived interest in pulsed ejectors (refs. 1 to 3), since the latter can increase the thrust, and potentially reduce the noise level, of such engines with little additional hardware. There have been measurements on pulsed ejector performance in the past, using drivers that were not detonation devices. Lockwood (ref. 4), using a pulsejet driver, measured thrust augmentations as high as 1.9, with a very short ejector. Didelle (ref. 5), using a jet interrupted by a butterfly valve, also observed a maximum thrust augmentation ratio of 1.9, but with a much longer ejector. Bertin (ref. 6), also claimed a thrust augmentation ratio of around 2, but gave few details. More recently, Paxson, Wilson, and Dougherty (ref. 7) have repeated Lockwood's experiment, with similar results, although the optimum ejector was rather longer than was Lockwood's. Wilson and Paxson (ref. 8), using a Hartmann-Sprenger, or resonance, tube to generate a pulsed jet, measured a maximum thrust augmentation of 1.32, and found, as did Paxson, Wilson and Dougherty, that there was an optimum radius for the ejector. Despite these efforts, it is still not clear what are the important parameters for optimizing a pulsed ejector. Except for that of Didelle, in none of the above experiments was the length of the pulse driving the ejector changed. Didelle, who varied the jet frequency, and hence pulse length, found his maximum thrust augmentation at a Strouhal number of 0.07.

A major feature of any pulsed jet flow is the starting vortex ring (Elder and deHaas (ref. 9), Das, Arekeri, Krothapalli, and Lourenco (ref. 10)). Gharib, Rambod, and Shariff (ref. 11) have shown that there is a critical value of the pulse length to diameter ratio L_{pulse}/D_{pulse} , which they called the formation number N: for values of $L_{pulse}/D_{pulse} < N$, the pulse transforms into a vortex ring only, for $L_{pulse}/D_{pulse} > N$, the flow becomes a vortex ring followed by a trailing jet. Since the structure of the flow changes in this way with L_{pulse}/D_{pulse} , one would expect that changing L_{pulse}/D_{pulse} might also affect ejector performance.

In order to explore this possibility, experiments to measure pulsed thrust augmentation were made using a shrouded Hartmann-Sprenger tube as the pulsed source. This source, previously used by Wilson and Paxson (ref. 8), has the advantage that by varying the tube and shroud lengths, different frequencies can be generated, corresponding to different values of the pulse length to diameter ratio. A statistical experiment was designed to explore the effects of ejector length, radius, and nose radius. This was repeated at each of four frequencies, and by fitting the data with a two parameter model, the effect of L_{pulse}/D_{pulse} and ejector radius on the thrust augmentation was determined. The maximum thrust augmentation was found to be at an L_{pulse}/D_{pulse} equal to the formation number, and the optimum ejector radius was found to be slightly smaller than the size of the vortex ring, defined as (R + a).

II. Apparatus

A photograph of the apparatus is shown in figure 1. Consisting of a shrouded Hartmann-Sprenger tube, a thrust plate, and a set of ejectors, it is the same as described by Wilson and Paxson (ref. 8), where a more detailed description will be found. The Hartmann-Sprenger tube (fig. 2) is a device which converts a steady, supersonic flow into a pulsed flow, by directing it into a resonance tube. It was shrouded to channel the pulsed flow into the axial direction. As initially built, the Hartmann-Sprenger tube operated at a frequency of 550 Hz. Different frequencies were obtained by, first, putting a plug inside the resonance tube to shorten it, which produced a frequency of 1100 Hz, and then making two longer tubes and shrouds to replace the original tube, to give frequencies of 275 and 125 Hz. Since the nozzle upstream of the resonance tube is choked, the mass flow remained the same for all frequencies.

The set of ejectors is also given in figure 2, to illustrate the geometry. The set includes four different ejector radii, R_{ej} , at each of which three lengths, L_{ej} , are possible, as well as three inlet radii, r_n . Since there was a diffuser on each ejector, the exit radius is greater than the ejector radius itself.

In running the experiment, the thrust of the jet without an ejector was measured, followed by the thrust with an ejector. The ratio of the two thrusts is the thrust augmentation α . The exact experimental procedure is described in Wilson and Paxson (ref. 8).



Figure 1. Photograph of the apparatus, showing the thrust plate at the top, the shrouded Hartmann-Sprenger tube at the bottom, and an ejector above it.

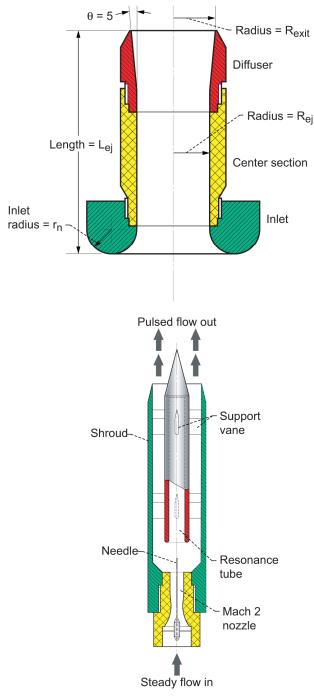


Figure 2. Schematic diagram of the Hartmann-Sprenger tube and the set of ejectors used in the experiment.

III. Design of the experiment

The original experimental design of Wilson and Paxson (ref. 8) for a frequency of 550 Hz was chosen to be a statistical design of experiments, three level, three parameter Box-Behnken scheme (ref. 12), with L_{ej}/R_s , $R_{ej}/R_{s,.}$ and r_n/R_s as the three parameters. This does not mean to imply that division by R_s is an appropriate scaling; it is simply a convenient way of making the numbers non-dimensional. Initially, the values of R_{ej}/R_s were 1.1, 1.5, and 3.0. As the

thrust augmentations for $R_{ej}/R_s = 3.0$ were small, it was found useful to add an additional group of ejectors with $R_{ej}/R_s = 2.0$, using $R_{ej}/R_s = 1.5$ as the "central" group. In making runs at a frequency of 1100 Hz, it was found that the optimum diameter for thrust augmentation appeared to be shifting towards lower values of R_{ej}/R_s , and so runs were made for $R_{ej}/R_s = 1.1$, 1.5, and 2.0 only, and not 3.0. As the frequency was lowered, the optimum shifted towards higher R_{ej}/R_s , and so the values of R_{ej}/R_s used were 1.5, 2, and 3, and not 1.1. The full set of runs made is given in table 1.

TABLE 1.—THE MATRIX OF TEST RUNS COMPRISING THE 3 PARAMETER,

	3 LEVEL S	STATISTICAL E	XPERIMENT	AT EACH OF T	HE FOUR FREC	QUENCIES US	ED
Run	R_{ej}/R_s	L_{ej}/R_s	r_n/R_s		C	ι	
No.				f=1100	f= 550	f= 275	f= 125
1	1.1	3.125	0.5	1.17	1.155		
2	1.1	7.125	0.25	1.149	1.16		
3	1.1	7.625	0.75	1.134	1.155		
4	1.1	12.375	0.5	1.122	1.092		
5	1.5	2.875	0.25	1.099	1.264		
6	1.5	3.375	0.75	1.053	1.275		
7	1.5	7.375	0.5	1.172	1.330		
8	1.5	7.375	0.5	1.167	1.325		
9	1.5	7.375	0.5	1.169	1.308		
10	1.5	12.125	0.25	1.166	1.255		
11	1.5	12.625	0.75	1.165	1.267		
12	2 2	3.125	0.5	1.022	1.118		
13	2	7.125	0.25	1.092	1.206		
14	2	7.625	0.75	1.10	1.226		
15	2 2	12.375	0.5	1.167	1.266		
16	3	3.125	0.5		1.034		
17	3	7.125	0.25		1.075		
18	3 3	7.625	0.75		1.085		
19	3	12.375	0.5		1.139		
20	1.5	3.125	0.5			1.287	1.14
21	1.5	7.125	0.25			1.320	1.221
22	1.5	7.625	0.75			1.355	1.237
23	1.5	12.375	0.5			1.326	1.265
24	2	2.875	0.25			1.277	1.186
25	2 2 2 2 2	3.375	0.23			1.343	1.218
26	2	7.375	0.73			1.379	1.317
27	2	7.375	0.5			1.373	1.295
28	2	7.375	0.5			1.376	1.313
29	2	12.125	0.25			1.305	1.271
30	2	12.625	0.25			1.383	1.310
50	2	12.023	0.73			1.505	1.510
31	3	3.125	0.5			1.053	1.075
32	3	7.125	0.25			1.106	1.137
33	3	7.625	0.75			1.116	1.182
34	3	12.375	0.5			1.197	1.250

IV. Experimental results

The measurements of thrust augmentation found in the various sets of Box-Behnken runs are given in table 1 and in figures 3 (a) to (d), in which thrust augmentation is plotted against normalized ejector length, L_{ej}/R_s , for each normalized ejector diameter, R_{ej}/R_s , at different values of the normalized nose radius, r_n/R_s . The 90 percent confidence level in α is \pm 0.03. The data from a Box-Behnken three parameter set can be fitted with a response surface of the form

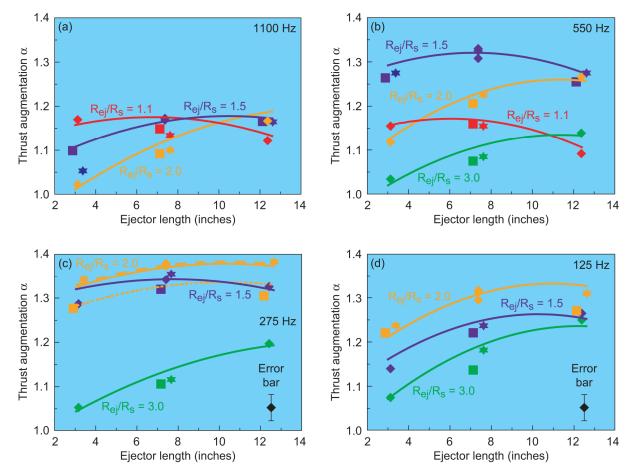


Figure 3. Results from the statistical experiments at four different frequencies. (a) 1100 Hz. (b) 550 Hz. (c) 275 Hz. (d) 125 Hz. Different symbols are used for each nose radius, \blacksquare , $r_n/R_s = 0.25$; \spadesuit , $r_n/R_s = 0.50$; \clubsuit , $r_n/R_s = 0.75$. Different colors are used for each ejector radius, red, $R_{ej}/R_s = 1.1$; dark blue, $R_{ej}/R_s = 1.5$; orange, $R_{ej}/R_s = 2.0$; green, $R_{ej}/R_s = 3.0$. The points are experimental data, the lines are response surface fits: dotted, $r_n/R_s = 0.25$; solid, $r_n/R_s = 0.50$; dashed, $r_n/R_s = 0.75$.

$$\alpha = b_{0} + b_{1} \cdot (L_{ej}/R_{s}) + b_{2} \cdot (R_{ej}/R_{s}) + b_{3} \cdot (r_{n}/R_{s}) + b_{11} \cdot (L_{ej}/R_{s})^{2} + b_{22} \cdot (R_{ej}/R_{s})^{2} + b_{33} \cdot (r_{n}/R_{s})^{2} + b_{12} \cdot (L_{ej}/R_{s}) \cdot (R_{ej}/R_{s}) + b_{13} \cdot (L_{ej}/R_{s}) \cdot (r_{n}/R_{s}) + b_{23} \cdot (R_{ej}/R_{s}) \cdot (r_{n}/R_{s})$$
(1)

where the values of the constants b_{ij} are determined from the data. These were found by inserting the data into a computer program (Seshadri and Demming (ref. 13)), which calculates the constants, and values of the confidence level for each constant. Constants with low confidence level were eliminated, until only terms with levels greater than 90 percent were retained. The resulting constants are listed in table 2. Once the response surface is known, the optimum thrust augmentation can be predicted, together with the values of L_{ej}/R_s , R_{ej}/R_s , and r_n/R_s at which the optimum occurs. These values are also listed in table 2.

TABLE 2.—CONSTANTS FOR EQUATION (1)—THE RESPONSE SURFACE OF THE BOX-BEHNKEN EXPERIMENTAL DESIGN, TOGETHER WITH PREDICTIONS FOR THE

	f=1100 Hz	f = 550 Hz	f=275 Hz	f= 125 Hz
b_{o}	1.16812	-0.18464	0.54744	0.32863
b_1	-0.01464	-0.00713		0.03207
b_2		1.81433	0.68699	0.64294
b_3	0.28836	0.23637	0.52521	0.44842
b ₁₁	-0.00126	-0.00197	-0.00103	-0.00193
b_{22}	-0.07511	-0.62527	-0.19356	-0.15947
b_{33}	-0.41306	-0.21744	-0.30355	-0.39603
b_{12}	0.02336	0.02591	0.01052	0.00505
b_{13}	0.01187			
b_{23}			-0.06310	
$lpha_{ ext{max}}$	1.189	1.331	1.385	1.338
R_{ej}/R_s	1.98	1.62	1.91	2.21
L_{ej}/R_s for α_{max}	12.6	8.9	9.9	11.2
r_n/R_s	0.5	0.5	0.75	0.5
L_{ej}/R_{ej}	6.36	5.49	5.18	5.07

Although equation (1) includes r_n , changes in α due to changes in r_n for the range of values used are very small, and the changes seen experimentally are statistically insignificant, except at a frequency of 275 Hz where for $R_{ej}/R_s = 2$, thrust for $r_n/R_s = 0.25$ seems lower than values for $r_n/R_s = 0.5$, and $r_n/R_s = 0.75$ indicating an optimum value between the latter two values. That, apart from this one case, changes in the nose radius seem unimportant is surprising, and may be a consequence of the limited values of r_n used in this experiment. Other experiments (refs. 7 and 15) have shown a significant effect of r_n , including the possibility of an optimum value. Sections through the response surface at each value of ejector radius, R_{ej} , for $r_n/R_s = 0.5$, are also plotted in figure 3, showing good agreement with the experimental results. The optimum values predicted are little different from the maximum observed experimental values.

V. Interpretation of the experimental results

A. Statement of the problem

It was originally hoped that by finding a response surface at each frequency, some insight would be gained into how the parameters affect the thrust augmentation as a function of the frequency. Except for the conclusion that changes in nose radius were not statistically significant, this was not apparent from the constants listed in table 2. Since the objective here is to find the overall maximum thrust augmentation, and at what values of the parameters this occurs, only the maximum augmentation achieved at any diameter, length and frequency will be considered further. These are listed in table 3. A more detailed look at these data is required.

TABLE 3.— L_{pulse}/D_{pulse} AND ε FOR EACH FREQUENCY USED, TOGETHER WITH THE MAXIMUM THRUST AUGMENTATION OBSERVED FOR EACH R_{ej} , TOGETHER WITH VALUES OF THRUST AUGMENTATION FOR $L_{pulse}/D_{pulse} = N$, I.E., $\alpha_{vr}|_{N}$, AND FOR $L_{pulse}/D_{pulse} = \infty$, I.E., α_{ss} , AS CALCULATED FROM

	TH	E VALUES OF	α AT $f = 275$, Al	ND f = 125.		
Frequency (Hz)	1100	550	275	125		0
L_{pulse}/D_{pulse}	2.5	5	10	22	6.86 = N	∞
ε	0.177	0.386	0.54	0.54	0.54	0.54
R/R_s	1.2438	1.313	1.3084	1.3084	1.3084	1.3084
α_{max} for $R_{ej}/R_s = 1.1$	1.17	1.16	-	-	-	-
α_{max} for $R_{ej}/R_s = 1.5$	1.169	1.321	1.355	1.265	1.395	1.191
α_{max} for $R_{ej}/R_s = 2.0$	1.167	1.266	1.376	1.308	1.406	1.252
α_{max} for $R_{ej}/R_s = 3.0$	-	1.139	1.197	1.25	1.174	1.294

B. Relationship of frequency to L_{pulse}/D_{pulse}

The experiments were performed at four different frequencies. Since the mass flow was constant at all frequencies, the mass per pulse m_{pulse} is given by

$$m_{pulse} = \dot{m}_{jet} / f \tag{2}$$

But m_p is also given by the product of pulse volume and density

$$m_{pulse} = \rho \pi D_{pulse}^2 L_{pulse} / 4 \tag{3}$$

from which it is seen that L_{pulse}/D_{pulse} is inversely proportional to frequency. In table 3 the values of L_{pulse}/D_{pulse} for each frequency used are given. Using the slug model plus some experimental measurements Wilson (ref. 14) has indicated that the value of the formation number is 6.86 for this shrouded Hartmann-Sprenger tube. Thus the two higher frequencies have values of L_{pulse}/D_{pulse} below the formation number, whilst the two lower frequencies have values of L_{pulse}/D_{pulse} above it.

C. Thrust augmentation for L_{pulse}/D_{pulse} greater than N.

For the measurements at values of L_{pulse}/D_{pulse} above the formation number, the flow consists of a leading vortex ring and a trailing jet. The vortex ring has exactly the same size and properties as that generated at $L_{pulse}/D_{pulse} = N$. The thrust on the ejector will be partially due to the vortex ring and partially to the trailing jet. There will be a time, t', following initiation of the jet at which the value of $L_{pulse} = \int u(t) dt$ is equal to $N.D_{pulse}$. The fraction of the total jet impulse that is in this portion of the jet is

$$p = \int_{o}^{t'} u(t)^2 dt / \int_{o}^{\tau} u(t)^2 dt$$
 (4)

It is this fraction of the impulse that goes into forming the vortex ring, giving rise to a thrust augmentation α_{vr} . The remaining impulse will be in the trailing jet, which will be assumed to create a thrust augmentation α_{ss} as would a steady jet. Thus, for L_{pulse}/D_{pulse} greater than the formation number, the total thrust augmentation will be

$$\alpha_{total} = p \, \alpha_{vr} + (1 - p) \alpha_{ss} \tag{5}$$

in which α_{vr} is calculated at the formation number, i.e., it is $\alpha_{vr}|_{N}$. A measurement of the jet exit velocity u(t) for this tube has been reported previously (Wilson (ref. 14)). Given this distribution, the integrals which determine p can be performed numerically. The result is given in table 4. Of course, if $L_{pulse}/D_{pulse} < N$, then $\alpha_{total} = \alpha_{vr}$, with no contribution from α_{ss} .

TABLE 4	.—VALUES	OF p AS .	A FUNCTION	OF L_{pulse}/D_{pulse}
				SPRÉNGER TUBE

L_{pulse}/D_{pulse}	6.86	7.4	8	10	12	14	16	18	20	22	24	∞
p =	1	0.9736	0.9424	0.8064	0.6724	0.5742	0.5002	0.4443	0.3990	0.3649	0.3363	0

At each of the two low frequencies, the value of p is known from table 4, i.e., p = 0.8064 at $L_{pulse}/D_{pulse} = 10$, and 0.3649 at $L_{pulse}/D_{pulse} = 22$. At each frequency, there are three values of α_{total} , one for each different ejector radius. Thus for each radius, there are two values of α_{total} , which can be substituted into an equation (5) for each frequency, so that the resulting pair of equations can be solved for $\alpha_{vr}|_{N}$, and α_{ss} . Values of $\alpha_{vr}|_{N}$, and α_{ss} are given in table 3. The values of α_{ss} for each ejector radius are fitted by the equation:

$$\alpha_{ss} = 1.094 + 0.158 \ln(2R_{exit}/D_{pulse})$$
(6)

As can be seen, α_{ss} increases as the ratio of ejector exit diameter to tube diameter increases. This trend, and the values of the thrust augmentation are in agreement with values of steady state thrust augmentation given by Porter and Squyers (ref. 16).

D. Thrust augmentation for L_{pulse}/D_{pulse} less than N

The objective of this work is to gain some understanding of the conditions which lead to maximum thrust augmentation, in particular ejector radius, and vortex ring size. Length is of course also an important parameter, but the value of $L_{ejector}/R_{ejector}$ at α_{max} , also given in table 2, and plotted in figure 4, does not appear to be very dependent

on L_{pulse}/D_{pulse} . At $L_{pulse}/D_{pulse} = N$, the value of $L_{ejector}/R_{ejector}$ for α_{max} is 5.2 – 5.5, and since from figure 3, at the maximum value of thrust augmentation for any of the curves, the augmentation does not depend strongly on ejector length, a value of $L_{ejector}/R_{ejector} = 5.3$ would probably be reasonably close to optimum at any frequency. To investigate the effects of ejector radius and vortex ring size, it was decided to use the values of maximum thrust augmentation observed at the two higher frequencies, together with the values calculated for $\alpha_{vr}|_N$ from the low frequency data, as the dependant parameter in creating a response surface in parameter space. A major question was what are the appropriate independent parameters to use in forming a response surface. Clearly, the thrust augmentation depends on the vortex ring properties, and the ejector size. Although L_{pulse}/D_{pulse} is important for vortex ring formation, once the ring is formed, the ratio ε is what characterizes it, and was chosen as the parameter for the vortex ring. For the ejector, the choice was not so clear. Considering the thrust augmentation, if the total exit flow from the ejector can be described by an average velocity in time and radius, V_{exit} , and the jet has an average velocity U such that $T_{jet} = \dot{m}_{jet} U$, then:

$$\alpha = \text{total thrust/thrust of jet alone}$$

$$= \dot{m}_{total} \ V_{exit} / \dot{m}_{jet} \ U$$

$$= \rho \pi (R_{exit} V_{exit})^2 / \rho \pi \xi (D_{pulse} \ U/2)^2$$

$$= (2 R_{exit} / D_{pulse})^2 (V_{exit} / U)^2 / \xi$$
(7)

from which:

$$V_{exit}/U = \sqrt{\alpha \xi} \left(D_{pulse} / 2 R_{exit} \right) \tag{8}$$

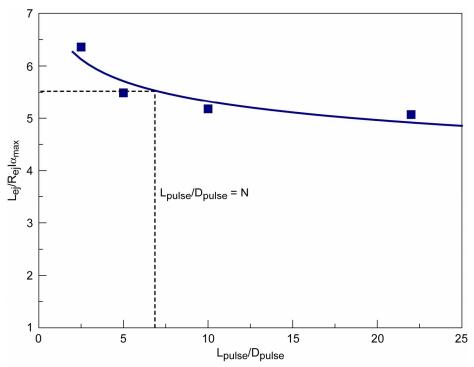


Figure 4. L_{ej}/R_{ej} at α_{max} versus L_{pulse}/D_{pulse} .

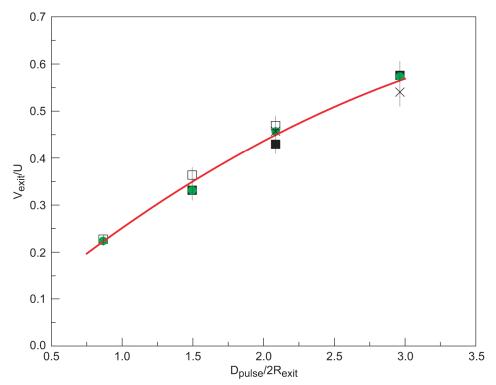


Figure 5. V_{exit}/U versus $D_{pulse}/2$ R_{exit} . \blacksquare $L_{pulse}/D_{pulse} = 2.5$, \bullet $L_{pulse}/D_{pulse} = 5$, \Box $L_{pulse}/D_{pulse} = 6.86$, calculated from measurements of α , \times $L_{pulse}/D_{pulse} = 5$, from direct measurement of V_{exit}/U .

Values of V_{exit}/U derived from equation (8) are plotted against $D_{pulse}/2R_{exit}$ for the points in table 3 with L_{pulse}/D_{pulse} less than or equal to N in figure 5, as well as two measured values of V_{exit}/U reported by Wilson and Paxson (ref. 8). Within the experimental error, these points are all fitted by a single line, shown in the figure. The equation of the line is:

$$V_{exit}/U = -0.123 + 1.442 D_{pulse}/2R_{exit} - 0.648 (D_{pulse}/2R_{exit})^2$$
(9)

This suggests that $D_{pulse}/2R_{exit}$ would be an appropriate parameter for fitting V_{exit}/U to the ejector size, from which the thrust augmentation could be obtained. Unfortunately, this did not prove to be the case, since small errors in fitting V_{exit}/U are magnified in calculating thrust augmentation, as it is the square of V_{exit}/U that appears in the equation for thrust augmentation. Nevertheless, the fit to V_{exit}/U is useful in calculating an estimate of the mass entrainment, since, as can be shown easily:

$$\alpha = (1 + \beta) V_{exit} / U \tag{10}$$

Instead of using the fit to V_{exit}/U , all the values of thrust augmentation given in table 3 were entered into a non-linear regression analysis with ε and one of either $D_{pulse}/2R_{exit}$, R/R_{exit} , or $(R+a)/R_{exit}$ as the independent parameters. It was found that the best fit was with $(R+a)/R_{exit}$ as the second parameter, with the resulting fit being:

$$\alpha = 1.816 - 3.743\varepsilon + 0.0389\varepsilon^{2} - 1.447(R+a)/R_{exit} + 0.679((R+a)/R_{exit})^{2} + 8.431\varepsilon(R+a)/R_{exit} - 4.014\varepsilon((R+a)/R_{exit})^{2}$$
(11)

Using this fit, together with thrust augmentation calculated from equation (5) for L_{pulse}/D_{pulse} greater than N, thrust augmentation is plotted against ejector radius in figure 6, and against L_{pulse}/D_{pulse} in figure 7. In using this fit,

the values of R and ε (and hence a) as a function of L_{pulse}/D_{pulse} were derived from slug theory as described by Wilson (ref. 14), R/R_s and ε are given in table 3.

VI. Discussion

These experiments indicate that a length of about two and a half times the ejector diameter is optimum. This is longer than claimed by Lockwood (ref. 4), but shorter than optimum length to diameter ratios found by Paxson, Wilson and Dougherty (ref. 7), or Didelle (ref. 5), The results given in table 2 for the optimum ejector length to diameter ratio seem to show a gradual decrease in the ratio as L_{pulse}/D_{pulse} increases. Thus the discrepancy in optimum ejector length to diameter between this work and those of Lockwood, and Paxson, Wilson and Dougherty might be explained as due to being in very different regimes of L_{pulse}/D_{pulse} . Didelle's maximum thrust augmentation was at a Strouhal number of 0.07. Because his valve gave two pulses per second, the value of L_{pulse}/D_{pulse} used by Didelle is $1/2S_t$, i.e., 7 at maximum thrust augmentation. Most of his runs were for $L_{pulse}/D_{pulse} < 7$, with a few at $L_{pulse}/D_{pulse} = 10$. It is gratifying that Didelle's optimum value of L_{pulse}/D_{pulse} is in close agreement with that found here, but that leaves the discrepancy of the optimum ejector length to diameter ratio unexplained.

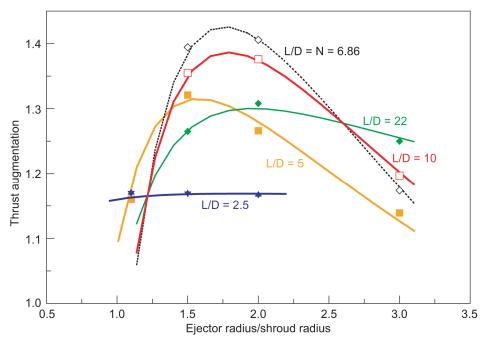


Figure 6. Thrust augmentation versus Rei/Rs.

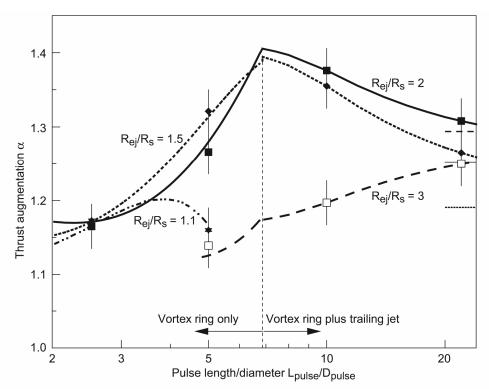


Figure 7. Thrust augmentation versus L_{pulse} / D_{pulse} for each value of R_{ej}/R_s . The thin horizontal lines at the right represent the values of α_{ss} . The data and fitted lines correspond to different values of R_{ej}/R_s , namely: $R_{ej}/R_s = 1.1$, —··—, *, $R_{ej}/R_s = 1.5$, ----, Φ , $R_{ej}/R_s = 2$, —, , \blacksquare , $R_{ej}/R_s = 3$, ---, \Box .

In these experiments, Didelle's experiments, and the experiments with pulsejet drivers, the length of the pulse increases with the inverse of the frequency, and so low frequency approaches steady state flow. Both Didelle (ref. 5), and Wilson and Paxson (ref. 8) found that V_{exit} had a large average component, with an oscillation on top of it, such that the ejector flow never reached zero velocity. Care must be used in relating the results to pulse detonation devices, where the pulse length is determined by the length of the tube, and is independent of frequency. Because the duty cycle is very low in detonation devices, V_{exit} may drop to zero between pulses. This is less likely as the frequency increases, and so high frequency is more likely to approach a steady state flow in the ejector.

VII. Conclusions

In conclusion, for the Hartmann-Sprenger tube investigated, unsteady thrust augmentation is shown to have a peak when the driving pulse jet has a pulse length to diameter ratio equal to the formation number. For values of L_{pulse}/D_{pulse} close to N, the optimum ejector radius will be equal to 0.87(R+a). As L_{pulse}/D_{pulse} increases, the optimum ejector radius also increases, until for very large values of L_{pulse}/D_{pulse} , the thrust augmentation approaches steady–state values, increasing monotonically with ejector radius. The optimum ejector length appears to be about 2.5 times the ejector diameter, although this does not agree with the results of other workers (refs. 4, 5, and 7).

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13. ABSTRACT (Maximum 200 words)

The thrust augmentation of a set of ejectors driven by a shrouded Hartmann-Sprenger tube has been measured at four different frequencies. Each frequency corresponded to a different length to diameter ratio of the pulse of air leaving the driver shroud. Two of the frequencies had length to diameter ratios below the formation number, and two above. The formation number is the value of length to diameter ratio below which the pulse converts to a vortex ring only, and above which the pulse becomes a vortex ring plus a trailing jet. A three level, three parameter Box-Behnken statistical design of experiment scheme was performed at each frequency, measuring the thrust augmentation generated by the appropriate ejectors from the set. The three parameters were ejector length, radius, and inlet radius. The results showed that there is an optimum ejector radius and length at each frequency. Using a polynomial fit to the data, the results were interpolated to different ejector radii and pulse length to diameter ratios. This showed that a peak in thrust augmentation occurs when the pulse length to diameter ratio equals the formation number, and that the optimum ejector radius is 0.87 times the sum of the vortex ring radius and the core radius.

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